

SPC
Class 1
Introduction
David Parent

Agenda

- Goals of the course
- Quality
- Control Charts
 - Why they are used
 - Example

Shewhart and Deming

The long range contribution of statistics depends not so much upon getting a lot of highly trained statisticians into industry as it does in creating a statistically minded generation of physicists, chemists, engineers, and other who will in any way have a hand in developing and directing the production processes of tomorrow.

Goals of this course

- Students should be able to
 - Speak the language of SPC
 - Incorporate its principles into designs
 - Know how to use an “SPC design flow”
 - develop a control chart or an acceptance procedure

More specifically

- Develop R, s, and p control charts
- know when to use each
- Use a control chart on data gathered in class to improve the 129 or 167 process line
- Use control charts to make decisions or reduce inspection costs

Quality

- quality of specification
- quality of conformance
- degree of excellence?
- quality (5 ohms)

Control chart fundamentals

- Measured quality of manufactured products is always subject to a certain amount of variation as a result of chance
- Some “system of chance causes” is inherent in any particular scheme of production and inspection
- Variation within a stable pattern is inevitable.
- The reasons for variation outside this stable pattern may be discovered and corrected.

Cooperation

- Design engineers and manufacturing engineers some times do not talk.
 - Specifications can be set tighter than the system can produce.
 - Specification can be pulled out of this air
 - SPC can show you what is possible and if what is possible will work! It come from hard data and not opinion!

Types of charts

- Xbar, R
- Xbar s
- fraction rejected (p)
- nonconforming (c)
- Variable
 - continuous length, width, current, power
- Attribute
 - counts or articles or events

Language

- Defect vs defective
- nonconformance: not meeting one specification
- percent rejected rather than percent defective

Control Charts

EE/MatE167

David W. Parent

Control Chart Design Flow

- I. Make decisions to prepare for control chart construction
 - A. Possible Objectives
 - B. Choose the variable
 - C. Decide on basis of subgroup
 - D. Choose size and frequency of subgroups
 - E. Set the data collection form
 - F. Determine method of measurement

Control Chart Design Flow

II. Start the control charts

- A. Make chart and record data
- B. Calculate \bar{X} and R for each subgroup
- C. Plot \bar{X} and R

Control Chart Design Flow

III. Determine trial control limits

- A. Decide on how many subgroups are required to calculate the limits
- B. Calculate trial control limits
- C. Plot the central lines and limits

Control Chart Design Flow

IV. Draw preliminary conclusions

- A. Decide whether in control or out
- B. Interpretation
- C. Discuss relationship between out of control processes and specification limits
- D. Suggest actions

Control Chart Design Flow

- V. Continue to use the charts
 - A. Revise central lines and limits
 - B. Sort lots
 - C. Decide on an action about a process
 - D. Acceptance inspection
 - E. Verify specifications

I-A Objectives

- Gather data
 - to verify specifications
 - verify production procedures
 - verify inspection procedures
 - justify current decisions
 - justify whether to hunt for problems
 - Learn control charts

I-B Variable

- Gather data that can
 - be measured in numbers
 - that can be used to save money or improve process

I-C sub group

- Choose subgroups that
 - are as homogenous as possible if you are trying to detect shifts in the process mean
 - are not homogeneous if acceptance testing

I-D Size of subgroup

- 4 is thought to be ideal
- 5 is easy to calculate
 - gets all area of a wafer
 - try to minimize variation in subgroup
- 2 or 3 if it is expensive
- 10-20 if we need a large sensitivity of shifts in the mean and standard deviation

Forms and method of measurements

- Forms
 - We will try to develop standard excel sheets so groups can share data
- Measurement
 - We have detailed instructions on how to use equipment

Example

- EE129 process
- Assume we are making simple current mirrors.

I-A Objectives

- What are the possible objectives?
- Or what are our main problems in EE/MatE129?
 - Currently we just make transistors to learn about processing, we don't make them for a given application
 - We want to change this so EE students can design circuits that are made in 129.

What do we need for a design environment?

- A process that is in control
- An idea of what specification limits the circuits designers can expect

More possible objectives (Current Decisions)

- Currently in 129 there is a lot of time spent measuring oxide thicknesses for etching, lab often goes over this time or students have to come back to do it.
 - We want to reduce time spent inspecting!
- Currently in the 129 process there is 8 microns of overlap to prevent device failures to to alignment
 - This caused the S/D area to be large
 - This causes device to be big, which limits how many devices we can put a on chip
 - More leakage
 - We need to verify this design rule!

More possible objectives

- Since we have not been doing control charts, we do not know if we have a problems, so lets not hunt for any.
 - If we find one, we find one.
- We need to learn control charts!

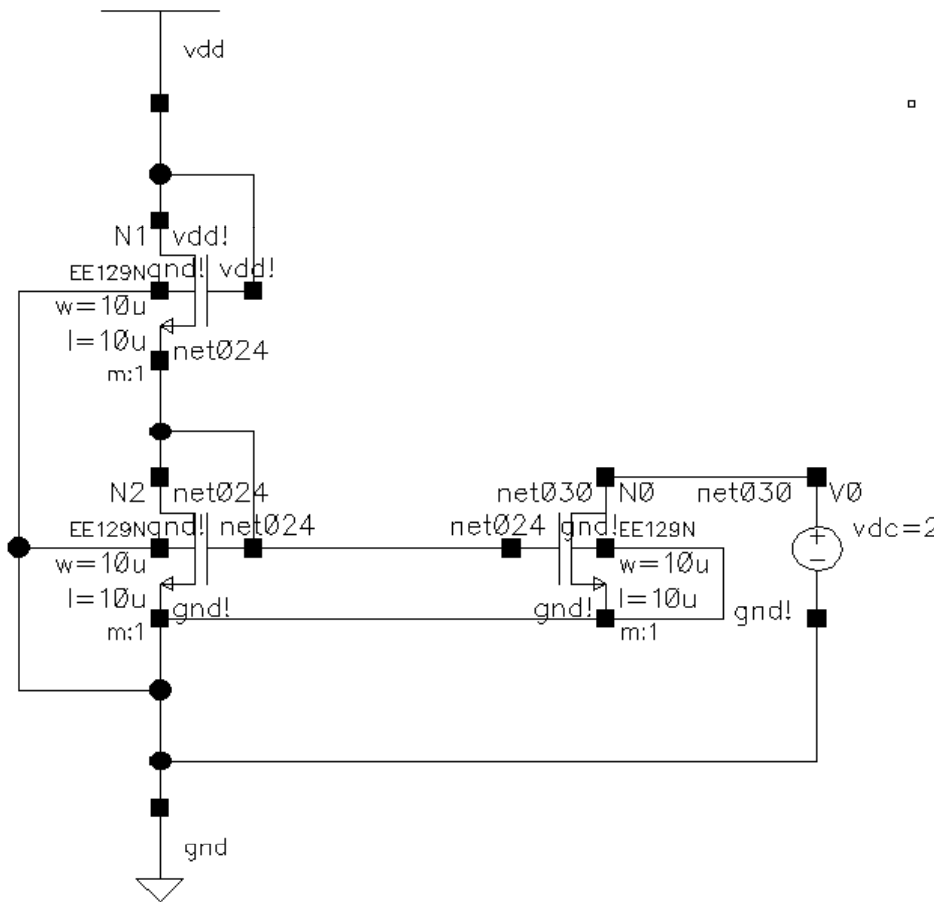
Choose the variable?

- What are the variables?
 - Wafer thickness
 - Wafer resistivity
 - Field oxide thickness
 - SOG Thickness
 - Gate oxide thickness
 - Diffusion resistivity
 - Junction depth
 - Contact resistivity
 - Metal height
 - Metal resistivity
 - mobility
 - KN
- Substrate doping
 - Junction capacitance
 - Channel width
 - Channel Length
 - V_T , fixed oxide charge
 - gamma
 - lambda (50 other bsim4 parameters)
 - Oxide breakdown
 - Junction Breakdown
 - Electromigration max current density
 - Metal1 Ndiff capacitance²⁷

There are 21 Variables in this simple 4 mask process!

- We need to narrow this number down.
- We need to compare the variables in terms of cost to measure, effect on the process, benefit we get from monitoring a particular variable.
 - Where do we start?
 - We go back to our product and the first order equations.

Our Product



$$I_{DSAT} = \frac{W}{2 \cdot L} \cdot \mu \cdot C_{ox} \cdot (V_{GS} - V_T)^2 \cdot (1 + V_{DS} \cdot \lambda)$$

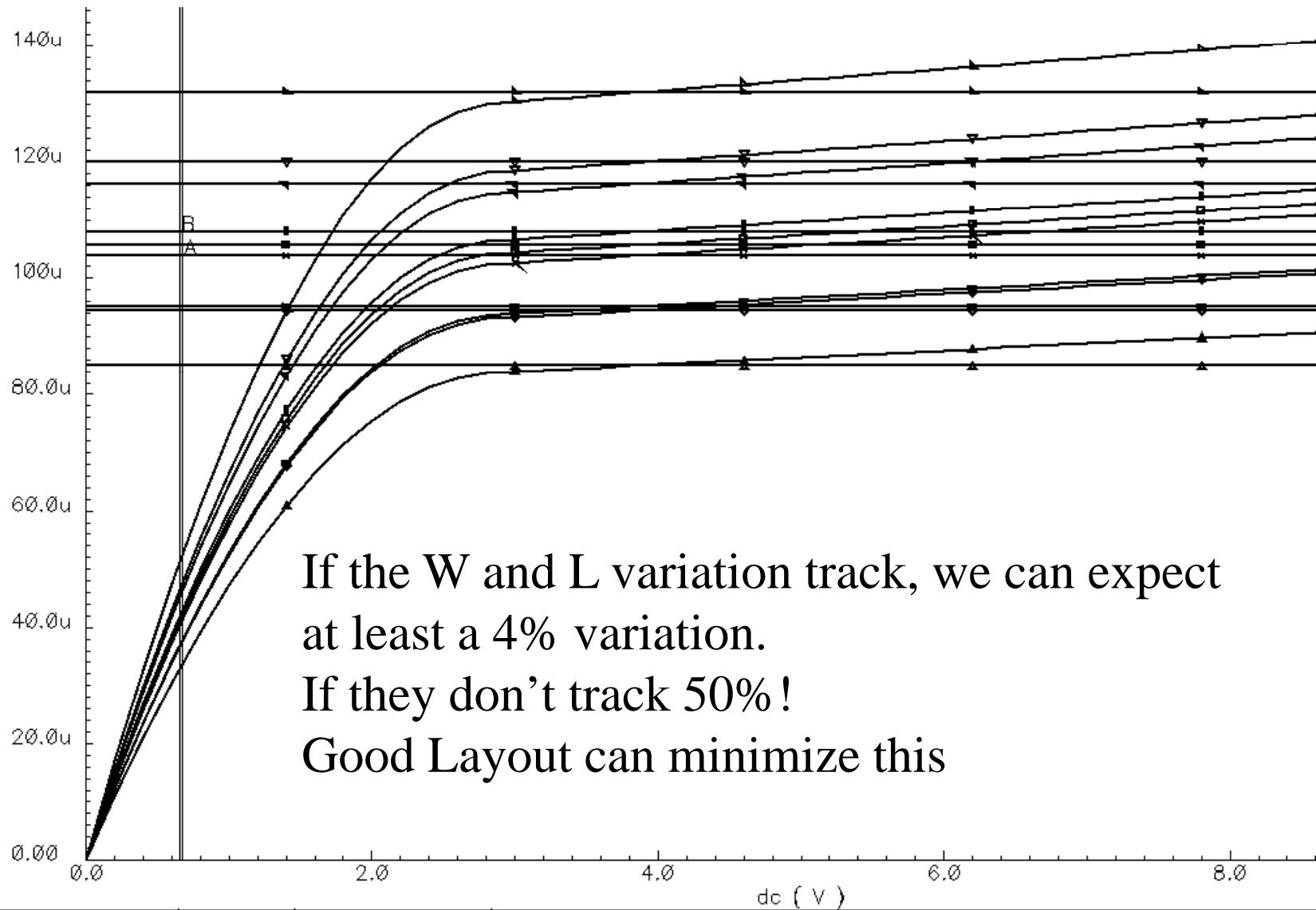
$$C_{ox} = \frac{\epsilon_{SiO2}}{T_{ox}}$$

$$V_T = V_{T0} + \gamma \cdot \left(\sqrt{|-2 \cdot \phi_F + V_{SB}|} - \sqrt{|2 \phi_F|} \right)$$

$$\gamma = \frac{\sqrt{2 \cdot q \cdot N_A \cdot \epsilon_{Si}}}{C_{ox}}$$

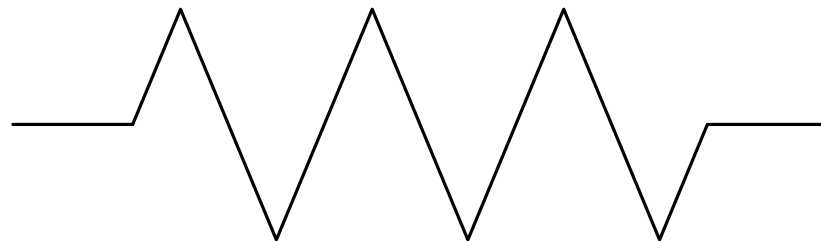
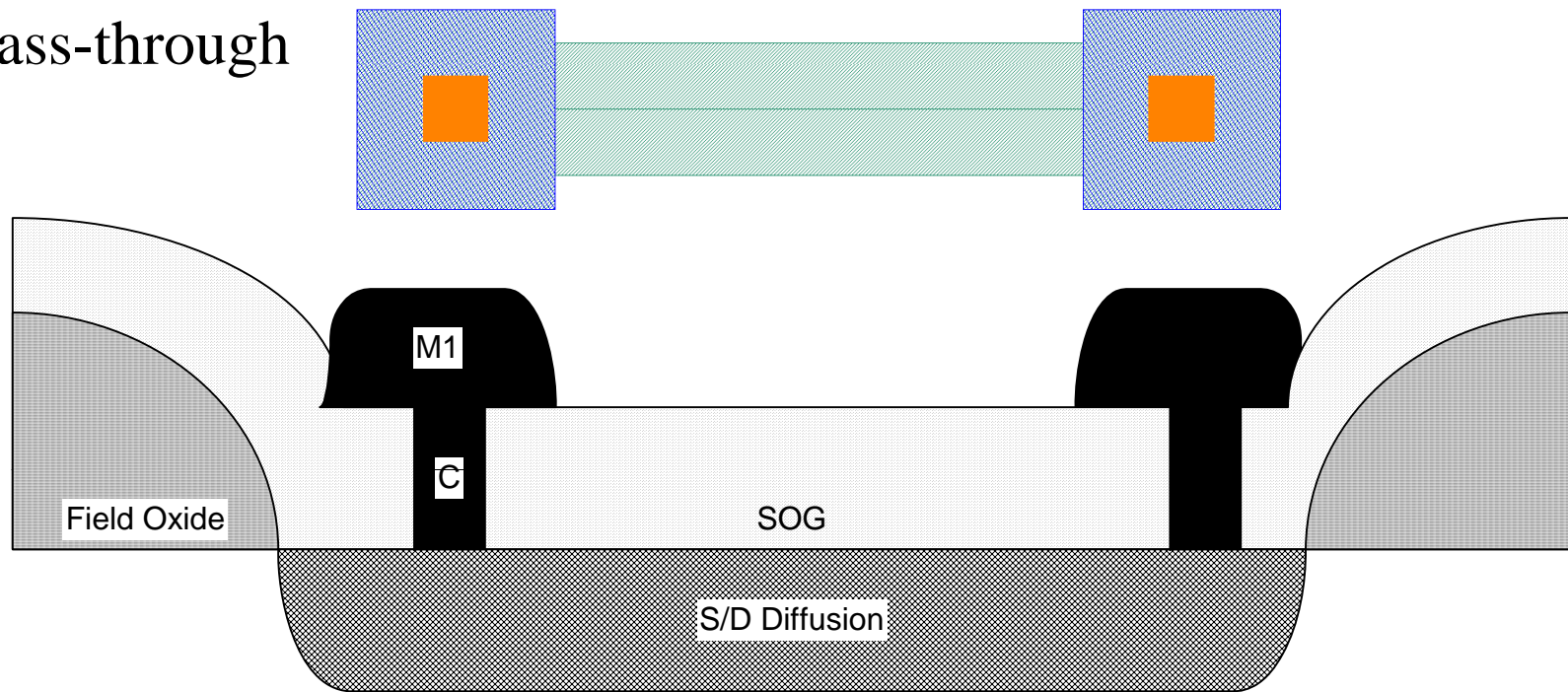
$$V_{T0} = \Phi_{GC} - 2 \cdot \phi_F - \frac{Q_B}{C_{ox}} - \frac{Q_{ox}}{C_{ox}}$$

$$Q_B = -\sqrt{2 \cdot q \cdot N_A \cdot \epsilon_{Si}} \cdot |2 \cdot \phi_F|$$

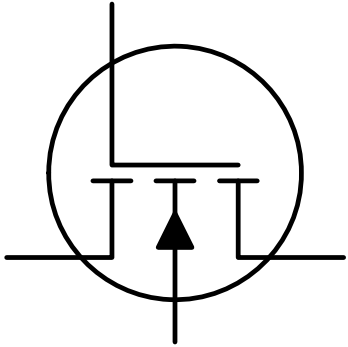
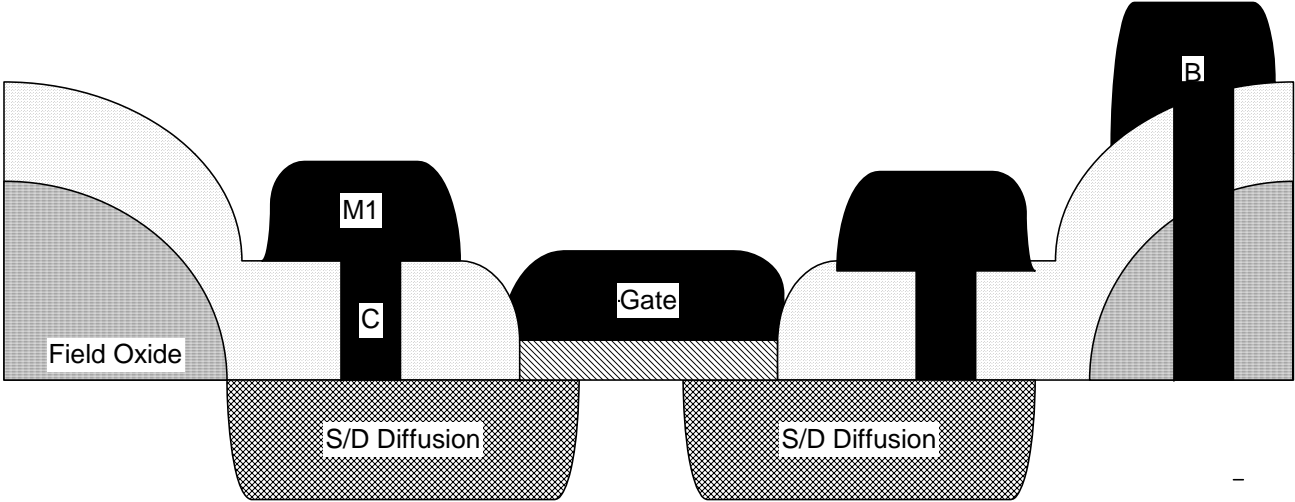
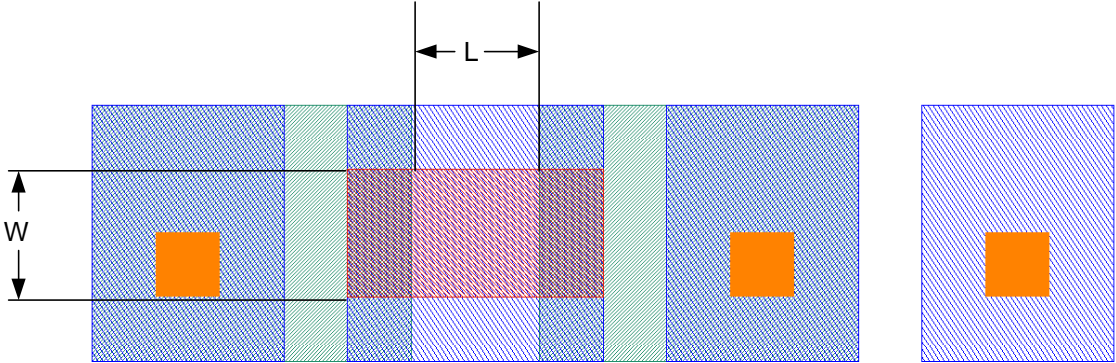


If the W and L variation track, we can expect
 at least a 4% variation.
 If they don't track 50%!
 Good Layout can minimize this

Resistor Pass-through



MOSFET



Modeling the MOSFET

$$\mu_N := 400 \frac{\text{cm}^2}{\text{V}\cdot\text{s}} \quad T_{\text{OX}} := .05 \cdot 10^{-4} \text{ cm}$$

$$C_{\text{OX}} := \frac{\epsilon_{\text{SiO}_2}}{T_{\text{OX}}}$$

$$\epsilon_0 := 8.85 \cdot 10^{-14} \frac{\text{F}}{\text{cm}}$$

$$K_{\text{NP}} := \mu_N \cdot C_{\text{OX}}$$

$$\epsilon_{\text{SiO}_2} := 3.9 \cdot \epsilon_0$$

$$K_{\text{NP}} = 2.761 \times 10^{-5} \frac{\text{A}}{\text{V}^2}$$

$$\lambda := .001 \text{ V}^{-1}$$

$$V_{\text{DS}} := 5 \text{ V}$$

$$V_{\text{T}} := 1 \text{ V}$$

$$I_{\text{DSAT}} := \frac{W}{2L} \cdot K_{\text{NP}} \cdot (V_{\text{GS}} - V_{\text{T}})^2 \cdot (1 + V_{\text{DS}} \cdot \lambda)$$

$$V_{\text{GS}} := 5 \text{ V}$$

$$W := 50 \cdot 10^{-4} \text{ cm}$$

$$I_{\text{DSAT}} = 1.11 \times 10^{-3} \text{ A}$$

$$L := 10 \cdot 10^{-4} \text{ cm}$$

VT0

$$\phi_{\text{ms}} := -0.6\text{V} - 0.0259\text{V} \cdot \ln\left(\frac{N_A}{n_i}\right) \quad Q_i := 5 \cdot 10^{10} \cdot \frac{\text{q}}{\text{cm}^2}$$

$$Q_D := -2 \cdot \left(\epsilon_{\text{Si}} \cdot \text{q} \cdot N_A \cdot \Phi_F\right)^{\frac{1}{2}}$$

$$V_{T0} := \phi_{\text{ms}} - \frac{Q_i}{C_{\text{ox}}} - \frac{Q_D}{C_{\text{ox}}} + 2 \cdot \Phi_F \quad +$$

$$V_{T0} = 1.035 \text{ V}$$

VT short channel

$$x_j := 2 \cdot 10^{-4} \text{ cm}$$

$$n_i := 1.5 \cdot 10^{-10} \text{ cm}^{-3}$$

$$x_{dD} := \sqrt{\frac{2 \cdot \epsilon_{Si}}{q \cdot N_A} \cdot (V_o + V_{DS})} \quad N_D := 1 \cdot 10^{20} \text{ cm}^{-3} \quad V_o := .0259 \text{ V} \cdot \ln\left(\frac{N_A \cdot N_D}{n_i^2}\right)$$

$$x_{dS} := \sqrt{\frac{2 \cdot \epsilon_{Si}}{q \cdot N_A} \cdot (V_o)}$$

$$x_{dD} = 5.605 \times 10^{-5} \text{ cm}$$

$$x_{dS} = 3.55 \times 10^{-5} \text{ cm}$$

$$L := 10 \cdot 10^{-4} \text{ cm}$$

$$\Delta V_{T0} := \frac{1}{C_{ox}} \cdot \sqrt{2 \cdot q \cdot \epsilon_{Si} \cdot N_A \cdot 2 \cdot \Phi_F} \cdot \frac{x_j}{2 \cdot L} \cdot \left[1 + \sqrt{1 + 2 \cdot \frac{x_{dS}}{x_j}} + \left(1 + \sqrt{1 + 2 \cdot \frac{x_{dD}}{x_j}} \right) \right]$$

$$\Delta V_{T0} = 0.605 \text{ V}$$

$$V_{T0} := V_{T0} - \Delta V_{T0} \quad V_{T0} = 0.43 \text{ V}$$

+

VT

- VT changes with VSB

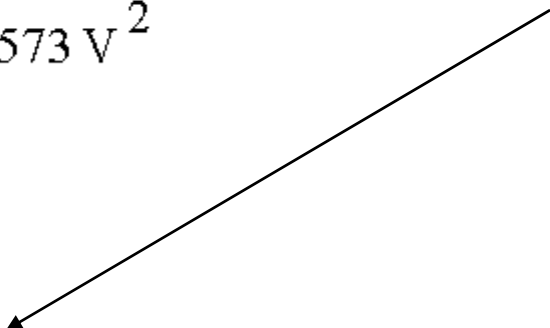
$$\gamma := \frac{\sqrt{2 \cdot \epsilon_{\text{Si}} \cdot q \cdot N_{\text{A}}}}{C_{\text{ox}}} \quad \gamma = 1.573 \text{ V}^{\frac{1}{2}}$$

$$V_{\text{SB}} := 5\text{V}$$

$$V_{\text{T}} := V_{\text{T0}} + \gamma \cdot \left(\sqrt{2 \cdot \Phi_{\text{F}} + V_{\text{SB}}} - \sqrt{2 \cdot \Phi_{\text{F}}} \right)$$

$$V_{\text{T}} = 2.835 \text{ V}$$

This will cause
trouble later.



Mobility

- Mobility changes with electric field
 - The constant μ_{NP} , is never constant
 - We use an average

λ

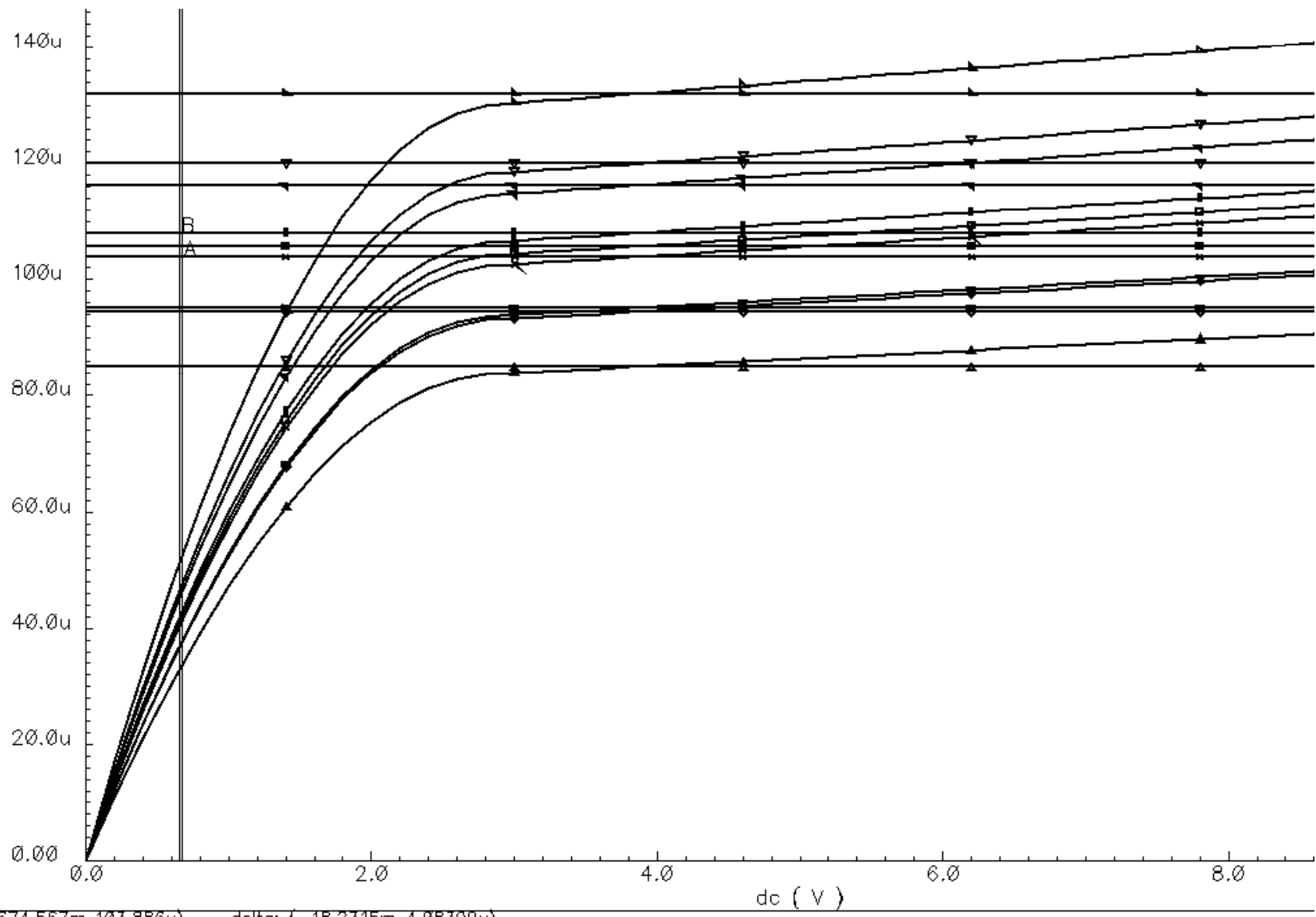
- This is due to the channel length narrowing.
 - The reversed biased diode's depletion region gets bigger with V_{DS} , and thus the length of the channel gets smaller, and thus the I_D goes up.

What does the circuit design engineer control?

- How big W and L are.
- How the wires are connected.
 - This does not sound like much is it is a lot.

What does the process design engineer control?

- T_{ox}
- N_a
- Junction Depth
- Q_i (kind of)



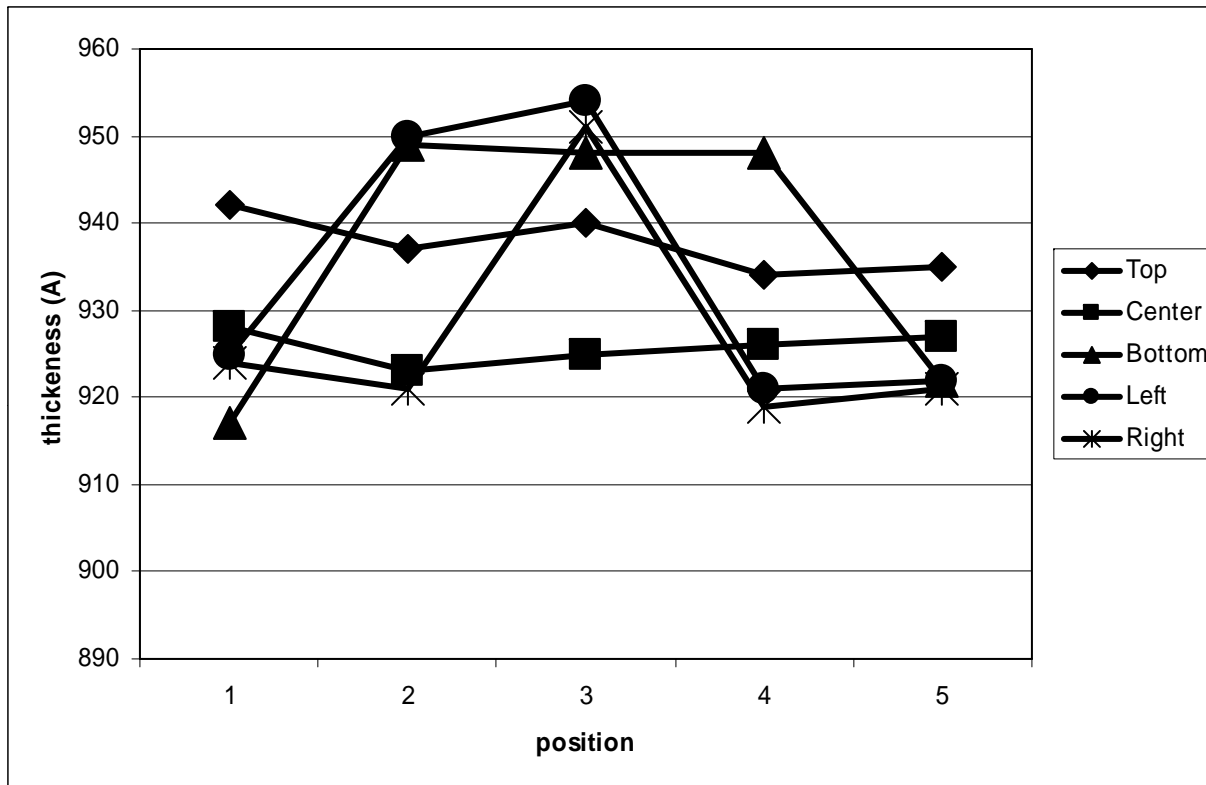
Will still need to decide the variable!

- We can see that gate oxide thickness is very important.
- It is easily measured
- It is measured early in the process

Choose the subgroup

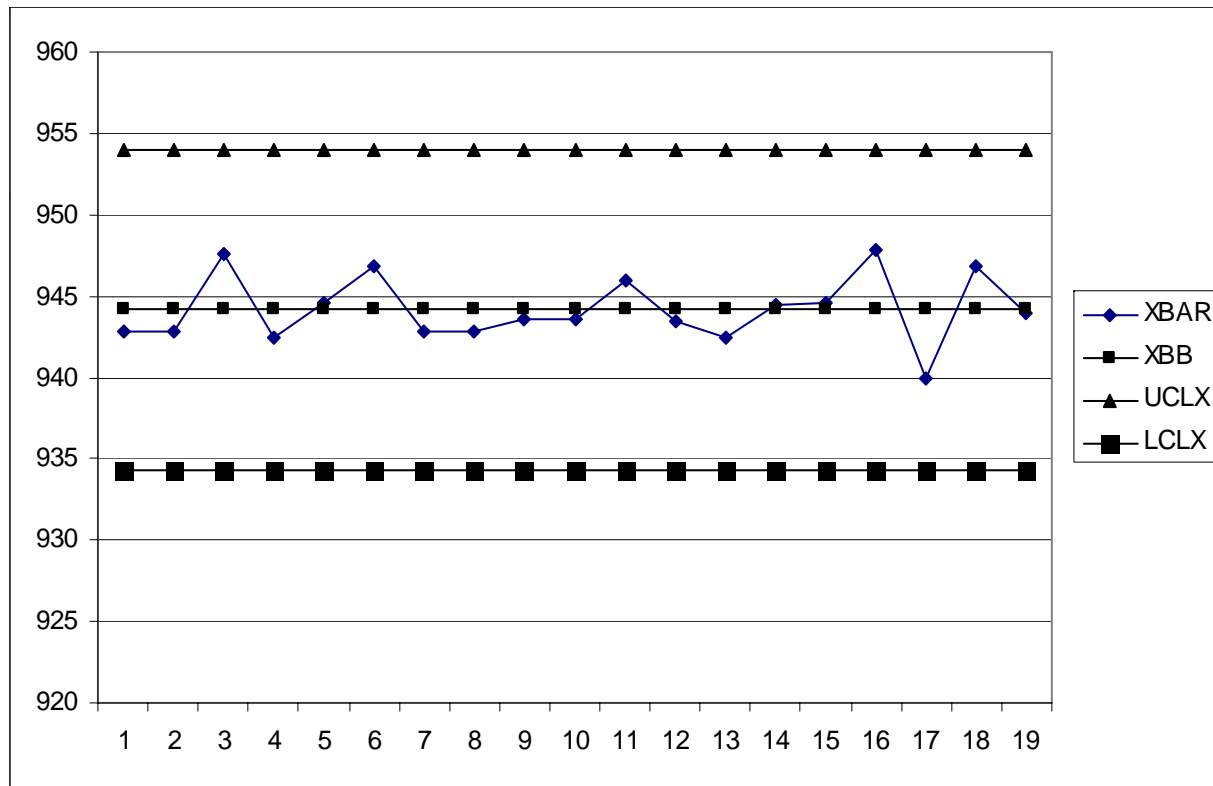
- We need to know how the oxide varies on the wafer, so we need to take 5 measurements on each wafer.
- The lots are not independent on wafer or in a single run of 50 wafers
- We still need to know if all wafers are within a spec limit so we need to measure each wafer in the batch
- After one run we can see trends and maybe we can take one reading per wafer or even every other wafer.
- We will choose to use all the readings from the center of each wafer.
- Since this will mean a subgroup of 10, we should use the \bar{X} , s (standard deviation) chart. We also want to use the \bar{X} s because we our product is analog and we need to be more sensitive to problems.

Preliminary Data



- There seems to be a trend with top and center, but the others are mixed.
- To minimize the variation within the subgroup we should take the top measurement from each wafer for the control chart. (We still need the other data for other things.)

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