

# Week 12 Semiconductor Conductivity Announcements

## Intrinsic Carrier Concentration as a Function of Temperature

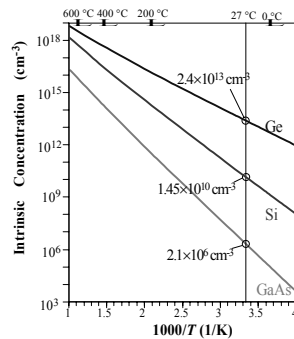


Fig. 5.16: The temperature dependence of the intrinsic concentration.

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# Ionization of Dopants

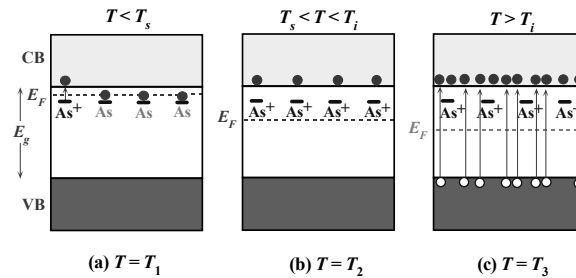


Fig. 5.14: (a) Below  $T_s$ , the electron concentration is controlled by the ionization of the donors. (b) Between  $T_s$  and  $T_i$ , the electron concentration is equal to the concentration of donors since they would all have ionized. (c) At high temperatures, thermally generated electrons from the VB exceed the number of electrons from ionized donors and the semiconductor behaves as if intrinsic.

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## Ionized Dopant Concentration

- If they aren't all ionized (low temperatures): need to calculate how many are ionized

$$n = \left( \frac{1}{2} N_C N_D \right)^{1/2} \exp\left( -\frac{\Delta E}{2kT} \right)$$

$$p = \left( \frac{1}{4} N_V N_A \right)^{1/2} \exp\left( -\frac{\Delta E}{2kT} \right)$$

- $\Delta E$  is the binding energy of the dopant

# Temperature Dependence of Carrier Concentration

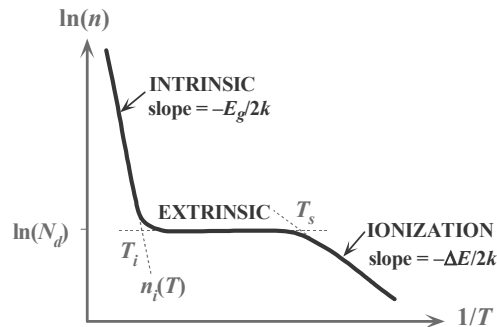


Fig. 5.15: The temperature dependence of the electron concentration in an n-type semiconductor.

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# Temperature Dependence of Dopant Concentration

- Low temperatures ( $T < T_s$ )
- Mid temperatures ( $T_s < T < T_i$ )
- High temperatures ( $T > T_i$ )

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## Temperature Dependence of Mobility

- Mobility also changes with temperature (which affects conductivity)
- Scattering as a function of temperature
  - Scattering increases due to increased thermal vibrations (same as metals)
- Scattering as a function of ionized impurities
  - How did impurities affect the conductivity of metals?
    - » Impurities (and other defects) acts as scattering sites for electrons because they disrupt the lattice
    - » Semiconductors have this affect: but the amount of impurity is minimal (in terms of lattice distortion and such)
  - Also have Coulombic scattering from ionized dopants

## Scattering from Lattice Vibrations

$$\tau_L = \frac{1}{Sv_{th}N_s} \propto \frac{1}{(T)T^{1/2}} \propto T^{-3/2}$$

## Scattering from Ionized Dopants

- As electrons pass ionized dopants they are attracted by Coulomb's Force (if the KE energy of the electron is less than this Coulombic PE)
  - get a critical radius (distance from ion that the electrons will be scattered)  $r_c$

## Critical Radius of Ionized Scattering

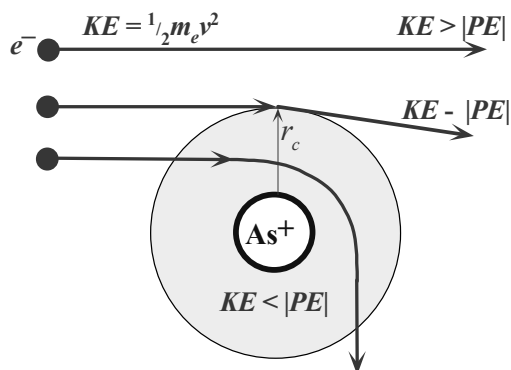


Fig. 5.17: Scattering of electrons by an ionized impurity

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## Scattering from Ionized Dopants

$$\frac{3}{2}kT = PE = \frac{e^2}{4\pi\epsilon_0\epsilon_r r_c}$$

$$r_c = \frac{e^2}{6\pi\epsilon_0\epsilon_r kT}$$

$$S = \pi r_c^2 = \frac{\pi e^4}{(6\pi\epsilon_0\epsilon_r kT)^2} \propto T^{-2}$$

## Mathiessen's Rule

# Temperature Dependence of Semiconductor Mobility

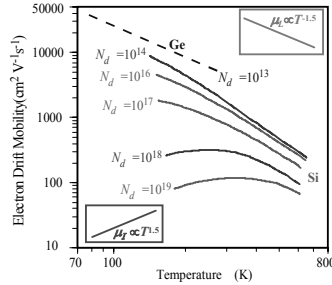


Fig. 5.18: Log-log plot of drift mobility vs temperature for *n*-type Ge and *n*-type Si samples. Various donor concentrations for Si are shown.  $N_d$  are in  $\text{cm}^{-3}$ . The upper right inset is the simple theory for lattice limited mobility whereas the lower left inset is the simple theory for impurity scattering limited mobility.

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# Concentration Dependence of Semiconductor Mobility

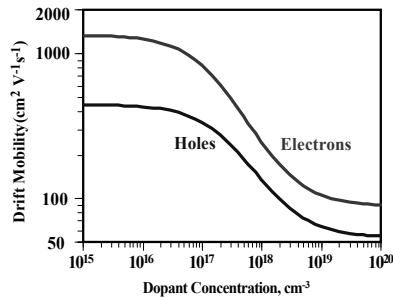


Fig. 5.19: The variation of the drift mobility with dopant concentration in Si for electrons and holes

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# Temperature Dependence of Semiconductor Conductivity

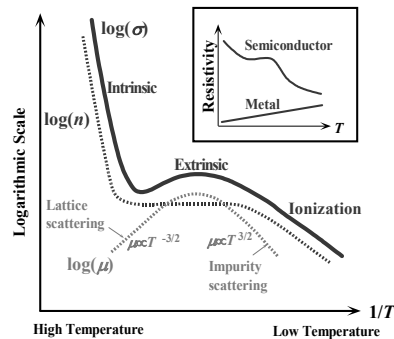


Fig. 5.20: Temperature dependence of electrical conductivity for a doped (*n*-type) semiconductor.

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## Temperature Dependence

- To understand temperature effect on semiconductor  $\sigma$  we need to combine the influence of free electron density ( $n$ ) and mobility ( $\mu$ )
- In the regions where  $n$  increases
- Where  $n$  is constant (mid temp region where dopants are saturated but intrinsic carriers are minimal)

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